## Accuracy \& Precision in Medicine How many digits do you keep?

## Determining accuracy \& precision of numbers

When you do calculations in a calculator, have you ever wondered how many digits you should keep? The answer is that it depends on the amount of digits that you put in, because your answer is only as precise as the least precise number that you put into your calculator.

The smaller the unit of measurement, the more precise the number is. Which number do you think is the most precise? 2.5 meters or 3.81 meters?

That's right - 3.81 meters is more precise because the person who measured used a tool that can measure to another decimal point. The more data you have, the more accurate your measurement.

What about this comparison. Which is more precise? 5.82 feet or 1.25 inches?
1.25 inches is more accurate because it measures the smallest scale division. If you think about 5.82 feet, that's actually 69.8 inches, so it has less precision than 1.25 inches.

This means that the first thing we need to talk about is precision in individual numbers.

## Determining the number of significant figures

If you are going to multiply the numbers, you need to identify how many are significant in the original values. To determine the number of significant figures follow these rules:

1. All non-zero numbers ARE significant

3456 has four significant figures, 198 has three significant figures
2. Captive zeroes ARE significant

309 or 400001 have captive zeroes as they are between non-zero numbers
3. Leading zeroes are NOT significant
ex. 0.00034 is only 2 significant figures, 0000125 is only 3 significant figures
4. For the zeroes at the end remember the rule: YES DOT, NO DOT NO

If there is a decimal in the number, the zeroes at the end are significant
If there is no decimal, they are not significant.
ex. 34000 is only 2 significant figures because the zeroes at the end represent a rounded value.
4.4000. is 5 significant figures because the zeroes at the end represent a measured value

TIP: If you have an exact number, add a decimal to the end to indicate that all of the digits are significant! For instance.... 2000 would be assumed to be rounded, so it has only 1 significant figure. If you have counted exactly 2000 of something, add a decimal at the end to indicate significance: 2000.

## Determining the final place of significance

If you are going to add or subtract the numbers, you need to identify the last place of significance To do this, find the last significant figure (using the directions above), then identify what place the last one is in. (100's, 10's, 1's, 10ths, 100ths... etc)

## References

http://www.ccpe-cfpc.com/en/pdf_files/drug_lists/normal_values.pdf

## Accuracy \& Precision in Medicine: Part 1

## Practice

Determine the number of significant figures for each value and its last place of significance. Using the internet, research each of the tests and fill in what the test is telling a person about their health. If it's within the normal values your diagnosis should be "normal".

| Parameter | Normal Values | Problem | \# of Sig | Last place of | Diagnosis |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Vital Signs |  |  |  |  |  |
| Heart Rate | 60-80 beats per minute (bpm) | Your patient has a heartbeat of 120 bpm . |  |  |  |
| Respiration Rate | 12-18 breaths per minute | Your patient has a body temperature of $39.6^{\circ} \mathrm{C}$ |  |  |  |
| Body Temperature | $36.5-37.5^{\circ} \mathrm{C}$ | Your patient's potassium levels are $2.9 \mathrm{mmol} / \mathrm{L}$ |  |  |  |
| Electrolytes |  | Your female patient has an RBC count of $3.1 \times 10^{12} / \mathrm{L}$ |  |  |  |
| Bicarbonate $\left(\mathrm{HCO}_{3}\right)$ serum | $24-30 \mathrm{mEq} / \mathrm{L}$ |  |  |  |  |
|  |  | Your patient has a white blood cell count of $1.5 \times 10^{5} / \mathrm{mm}^{3}$ |  |  |  |
| Chloride Serum | 98-106mEq/L |  |  |  |  |
| Potassium | $3.5-5.0 \mathrm{mmol} / \mathrm{L}$ | Your patient's aldosterone level is at $38 \mathrm{ng} / \mathrm{dL}$ |  |  |  |
| Sodium serum | $135-145 \mathrm{mEq} / \mathrm{L}$ |  |  |  |  |
| HEMATOLOGICAL PARAMETERS |  | Your patient's insulin level is at $4 \mu \mathrm{U} / \mathrm{L}$ |  |  |  |
| Red Blood Count (RBC) (Erythrocytes) | Female: <br> $4.0-5.2 \times 10^{12} / \mathrm{L}$ <br> Male: <br> $4.2-5.7 \times 10^{12} / \mathrm{L}$ | Your patient's Thyroid Stimulating Hormone levels are at $0.12 \mu \mathrm{U} / \mathrm{mL}$ |  |  |  |
| Hemoglobin | Female: <br> $12.3-15.7 \mathrm{~g} / \mathrm{dL}$ <br> Male: <br> $14.0-17.4 \mathrm{~g} / \mathrm{dL}$ | Your patient has a respiration rate of 8 breaths per minute |  |  |  |
|  |  | Your patient's sodium serum level is at $38 \mathrm{mEq} /$ L |  |  |  |
| White Blood Cell Count | $4.0-10.0 \times 10^{3} / \mathrm{mm}^{3}$ |  |  |  |  |
| Platelet Count | $130-400 \times 10^{3} / \mathrm{mm}^{3}$ | Your male patient's hemoglobin levels are at $12.8 \mathrm{~g} / \mathrm{dL}$ |  |  |  |
| Hormones |  |  |  |  |  |
| Aldosterone | $19-34 \mathrm{ng} / \mathrm{dL}$ | Your female patient's estrogen level is at $125 \mathrm{pg} /$ mL |  |  |  |
| Estrogens (as Estradiol) | Female: $50-450 \mathrm{pg} / \mathrm{mL}$ |  |  |  |  |
| Insulin | 5-25 $\mu \mathrm{U} / \mathrm{L}$ | Your male patient's testosterone level is at 825 ng/dL |  |  |  |
| Testosterone | Female: <br> $<62 \mathrm{ng} / \mathrm{dL}$ <br> Male: <br> 300-1000ng/dL |  |  |  |  |
| Thyroid Stimulating Hormone | $0.4-5.0 \mu \mathrm{U} / \mathrm{mL}$ |  |  |  |  |

## Accuracy \& Precision in Medicine

How many digits do you keep?

## Adding \& Subtracting - Based on place of significance

When you add or subtract a number you are essentially doing the same mathematical function, since subtracting is the same as adding a negative number.
If you think about how you line up numbers to add them together, you always line them up using the decimal.

$$
\text { Try this problem: 2.314inches }+87.6 \text { inches }=?
$$

Your calculator will give you the answer 89.914inches, however, that answer does not match the accuracy of our measured values.

Set up the problem like you learned in elementary school...
 89.9

If you look closely at the way you do basic addition, you will notice that it's lined up so that you add the same place with its place. (10ths +10 ths, 100 's +100 's, etc). This means that the last significant place in your values you are adding together determines the how many digits you keep in your final answer.

Because most of the values we use have a decimal, this rhyme may help: When you ADD look at the DAD (Digits After Decimal). Whichever value has the least DAD's will determine your rounding of the answer.

## References

http://www.ccpe-cfpc.com/en/pdf_files/drug_lists/normal_values.pdf

## Accuracy \& Precision in Medicine: Part 2

## Practice Addition Accuracy

| Problem - Underline the last digit in <br> each number | Calculator answer: Underline the <br> last digit you can keep | Accurate Answer: <br> Rounded |
| :---: | :--- | :--- |
| $31.5+0.1 \underline{7}$ | 31.67 <br> *This gets rounded up because the <br> next number is over 5. | 31.7 |
| $2 \underline{8} 00+12 \underline{5} 0$ | $4 \underline{5} 50$ <br> *We round everything after the last <br> digit you can keep and turn it to a <br> zero |  |
| $12.89+123$ |  | 4100 |
| $357+1.56$ |  |  |
| $200+1$ |  |  |
| $200 .+1+24$ |  |  |
| $78.3-1.005$ |  |  |
| $2.98-31$ |  |  |
| $45-0.921$ |  |  |

Multiplying and Dividing - Based on the number of significant figures
In order to determine the number of digits you will use when you multiply or divide, you merely need to determine the number of significant figures in each of the initial values. The calculator answer is then rounded to have the same number of significant figures as the least of your initial values.

## Practice Multiplication Accuracy

| Problem - Underline all significant <br> figures in each number | Calculator answer: Underline the significant <br> figures you can keep | Accurate Answer: <br> Rounded |
| :---: | :---: | :---: |
| $\underline{418 \times 0.31}$ | *This gets rounded up because the next <br> number is over 5. | 120 |
| $\underline{3805 \times 0.00540}$ | $\underline{20.547}$ | 20.5 |
| $1.584 \times 3200$ |  |  |
| $7100 \times .25$ |  |  |
| $35007 \times 0.00019$ |  |  |
| $100 \times 0.523$ |  |  |
| $67 \times 90$ |  |  |

## Medical Application Problems

Solve each problem using the correct rules from the lesson

1. A nurse adds 5.0 mL to an IV bag containing 250 mL . How many mL are now in the IV bag?
2. A patient's blood sample is 8.5 mL , and 3 drops of a chemical are added to test the solution. Each drop is 0.05 mL . What is the final volume of the solution?
3. A doctor has ordered 1.5 liters of normal saline for a patient. If it has to be given over 10 hours, how many liters per hour will drip into the patient's IV?
4. A patient is going to take 12 mL of cough syrup each night and the doctor gives the patient a bottle containing $100 . \mathrm{mL}$. How many doses of cough syrup are in the bottle?
